

EC-301 Computer Graphics

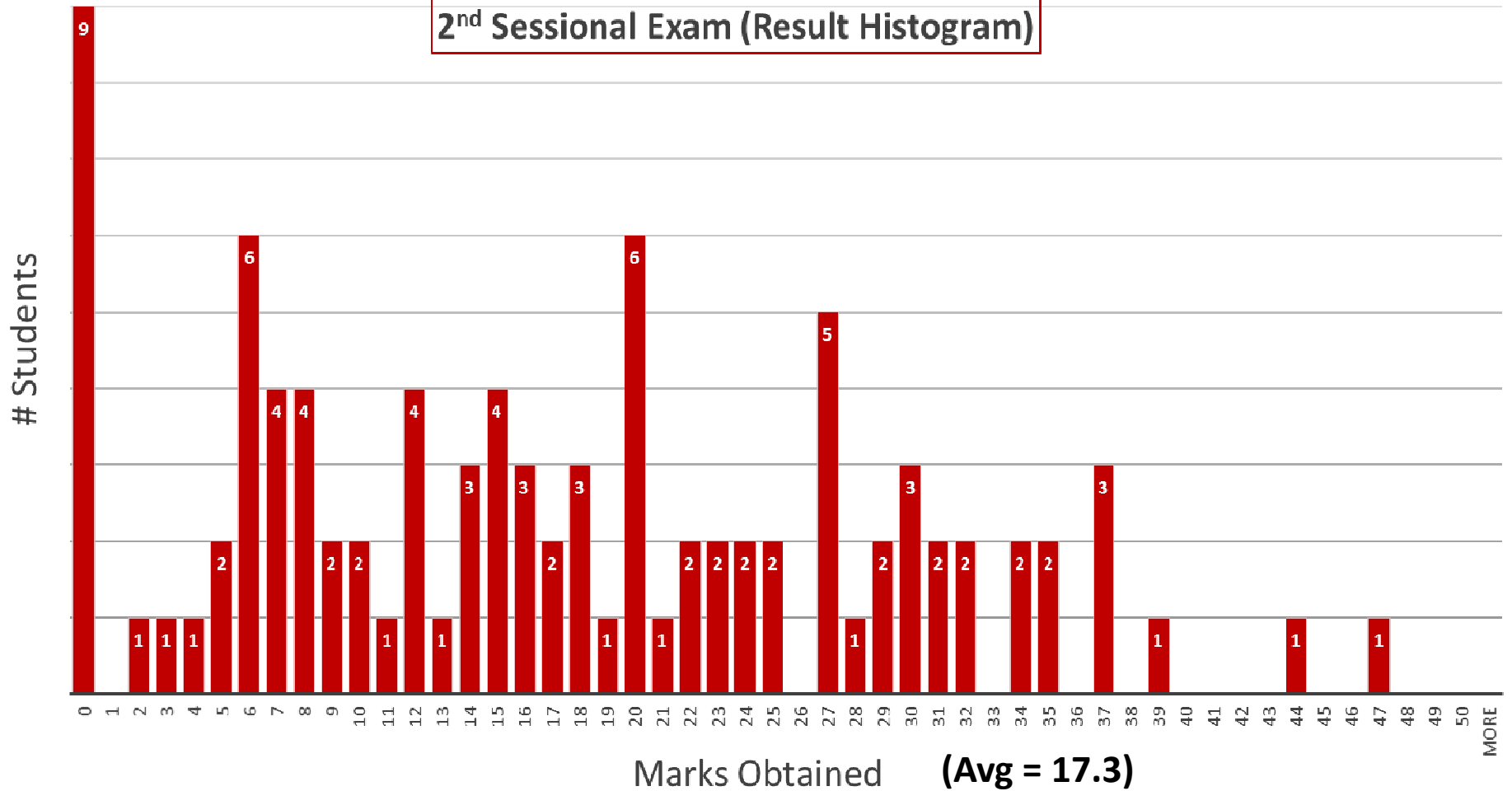
Lecture Slides- Wk16&17:

- Revised Grading Policy
- Result Histogram- 2nd Sessional Exam
- Two-Dimensional Viewing

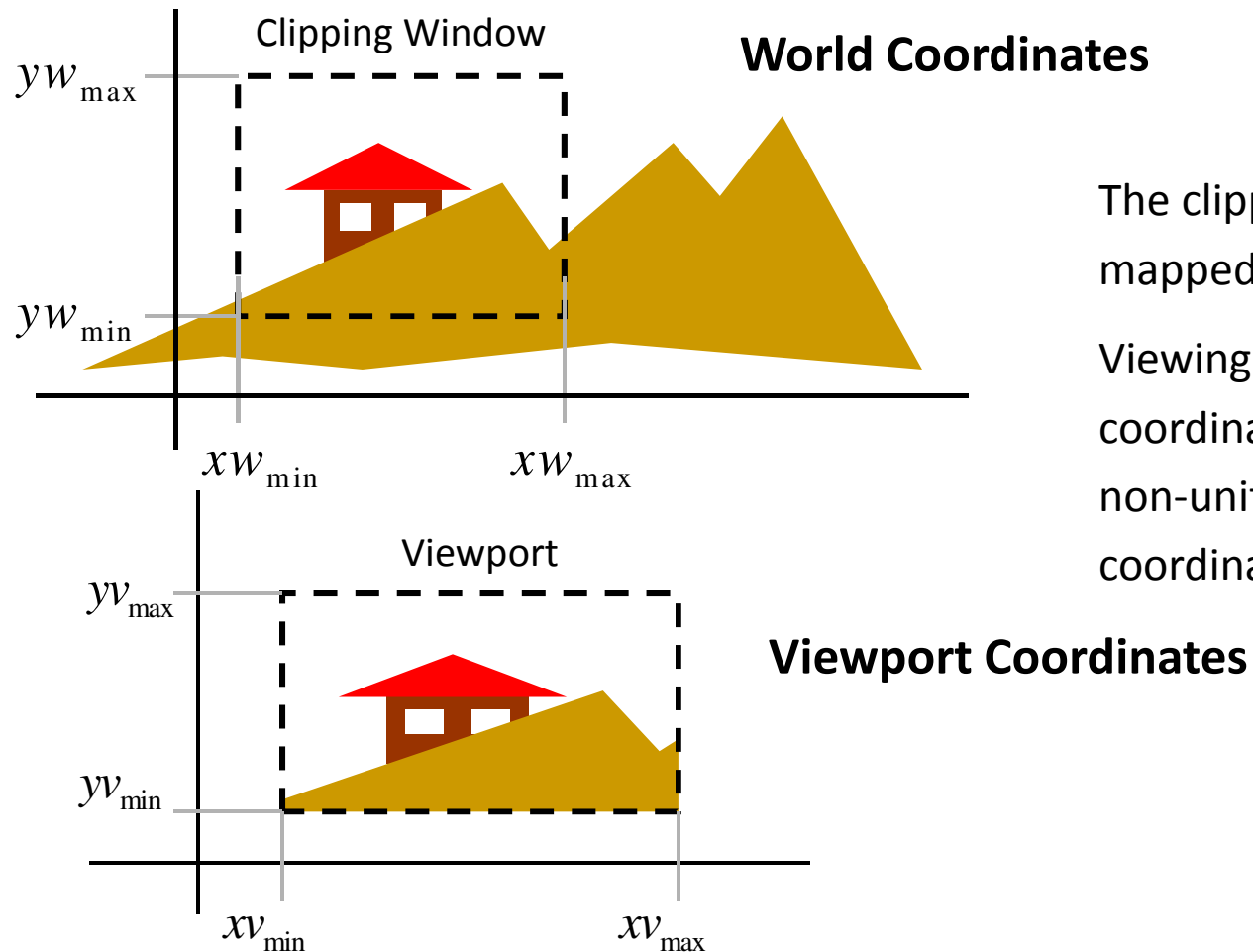
Revised Grading Policy

- Class Quizzes (Min 3) 6.7%
- Lab Tasks 5%
- Lab Assignmtns/Quizzes 6.4%
- Project 15%
- Final Lab 6.6%
- Sessional Exam-I 13.4%
- Sessional Exam-II 13.4%
- Final Exam 33.5%

EC301 Computer Graphics
2nd Sessional Exam (Result Histogram)



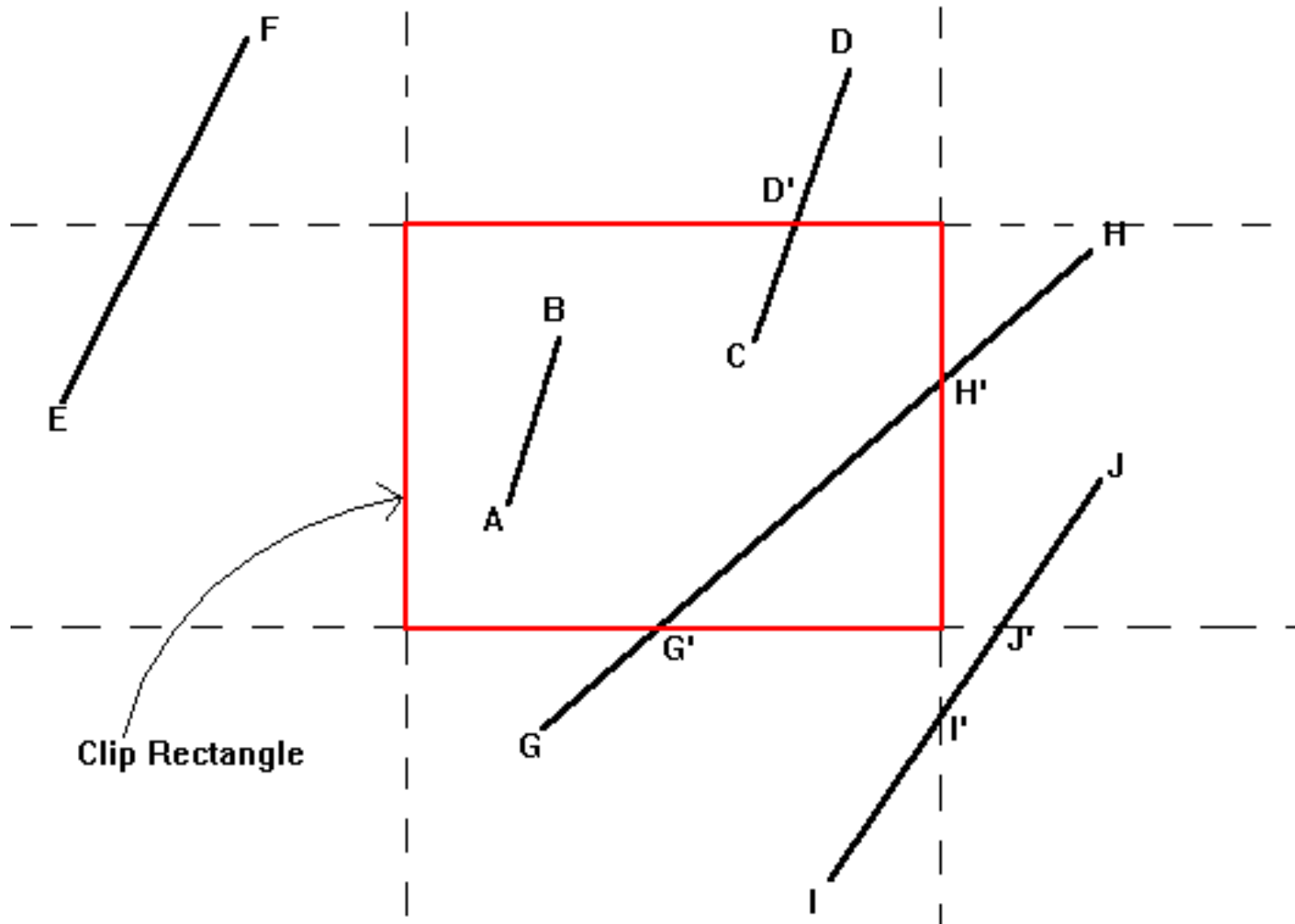
Two-Dimensional Viewing

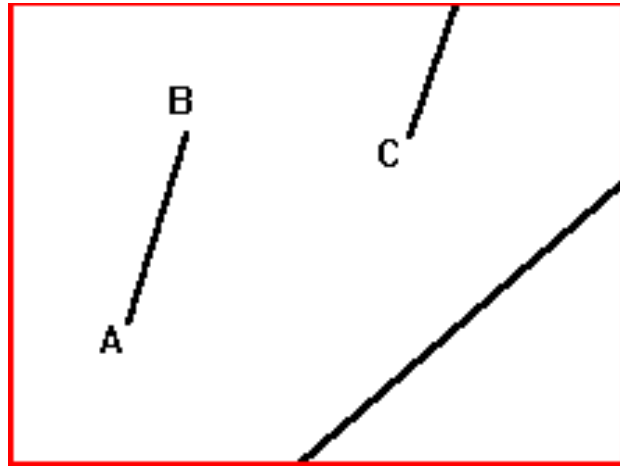


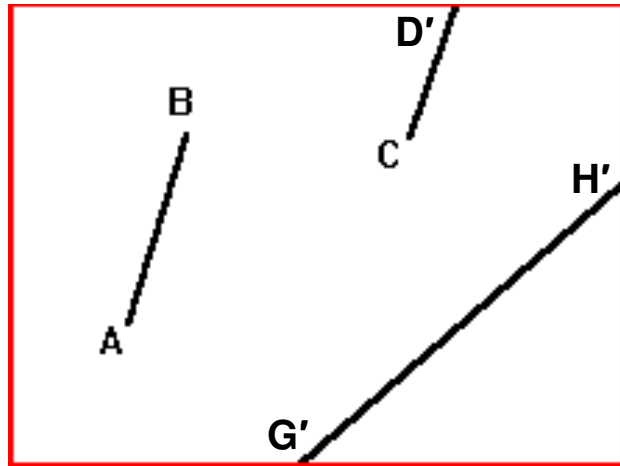
The clipping window is mapped into a viewport.

Viewing world has its own coordinates, which may be a non-uniform scaling of world coordinates.

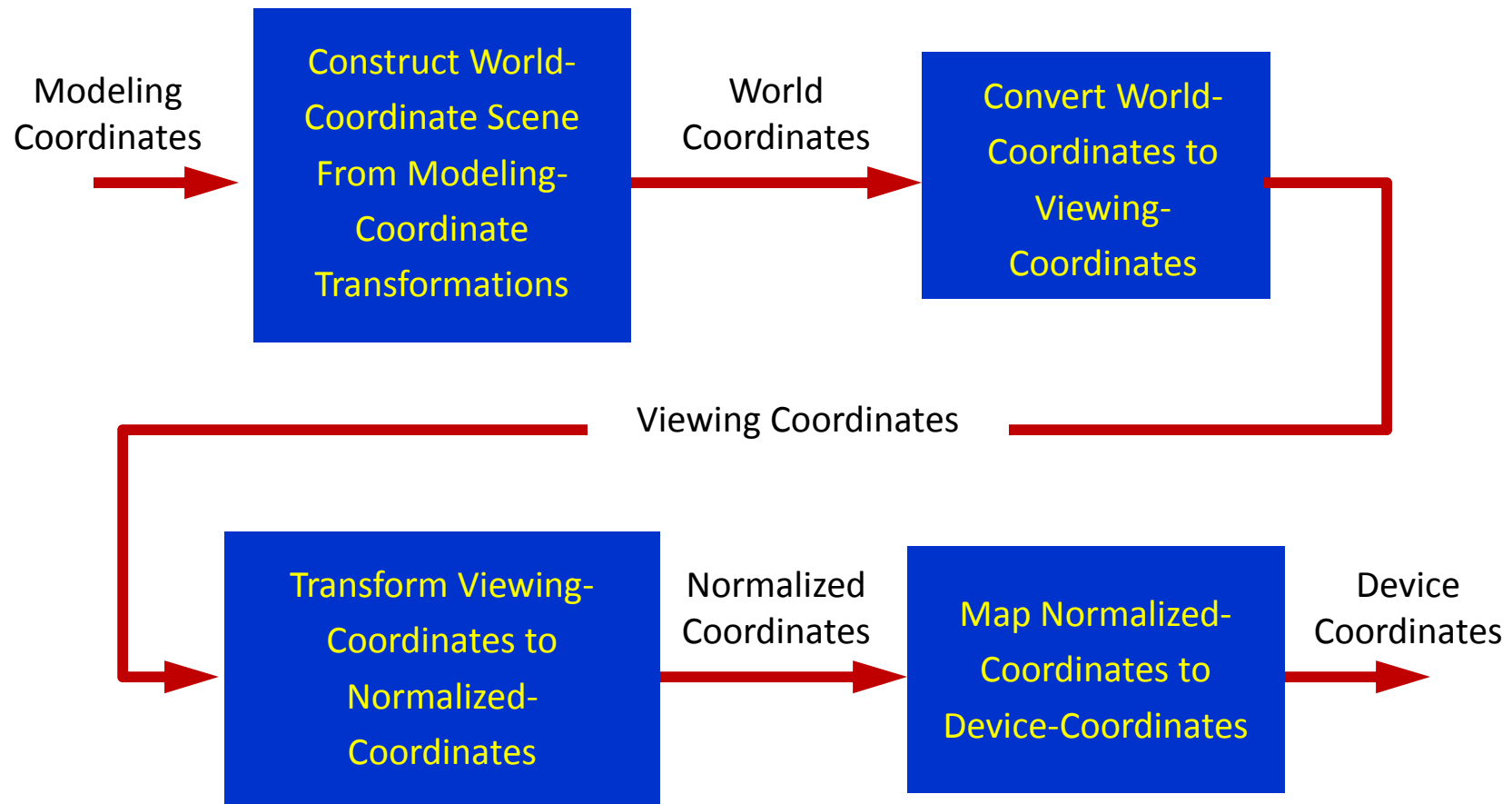
The clipping window selects what we want to see; the viewport indicates where it is to be viewed on the output device.



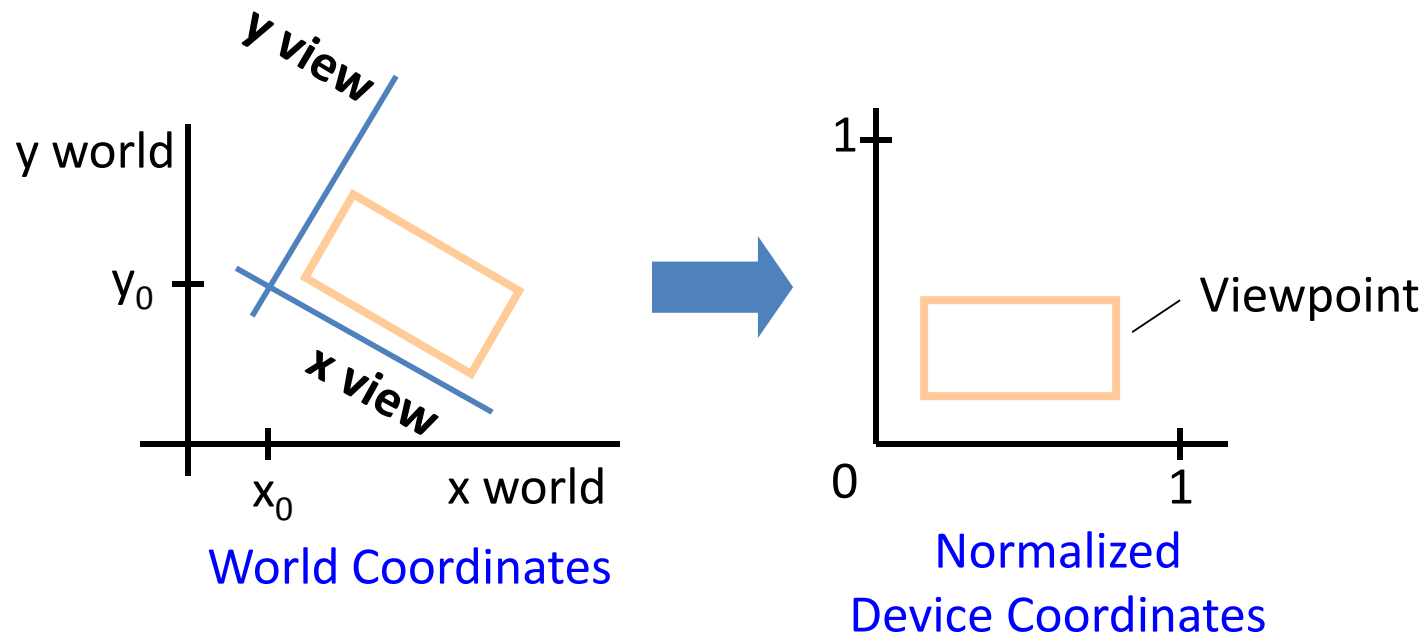




2D Viewing Transformation Pipeline



- Setting up a rotated world window in viewing coordinates and the corresponding normalized-coordinate viewport



Viewing Coordinate Reference Frame

- Used to provide a method for setting up arbitrary orientations for rectangular windows
- Matrix for converting world-coordinate positions to viewing coordinate

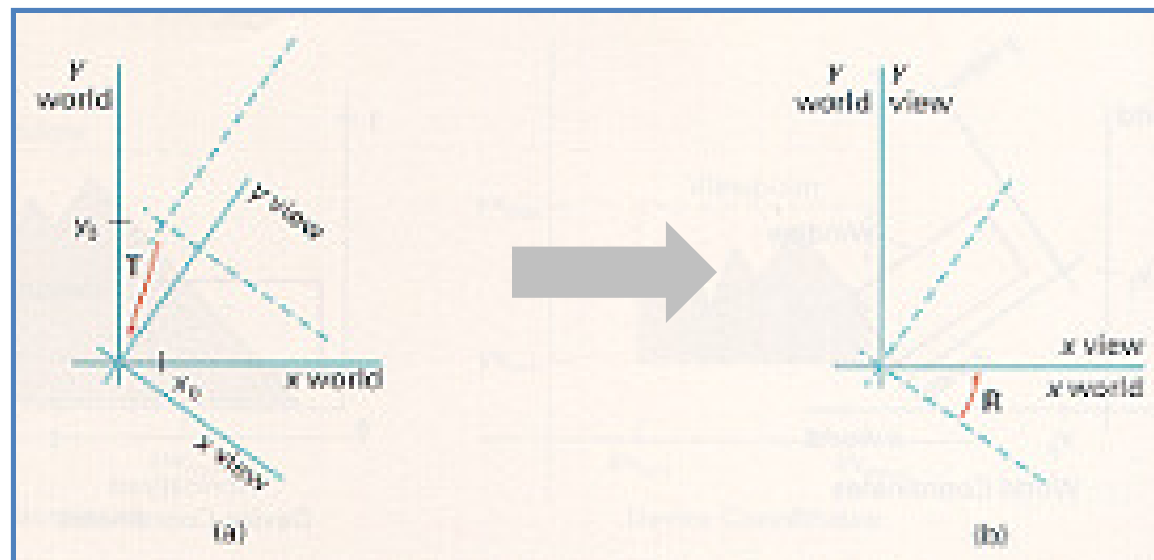
$$\mathbf{M}_{WC,VC} = \mathbf{R} \cdot \mathbf{T}$$

R: rotation matrix

T: translation matrix

Viewing Coordinate Reference Frame

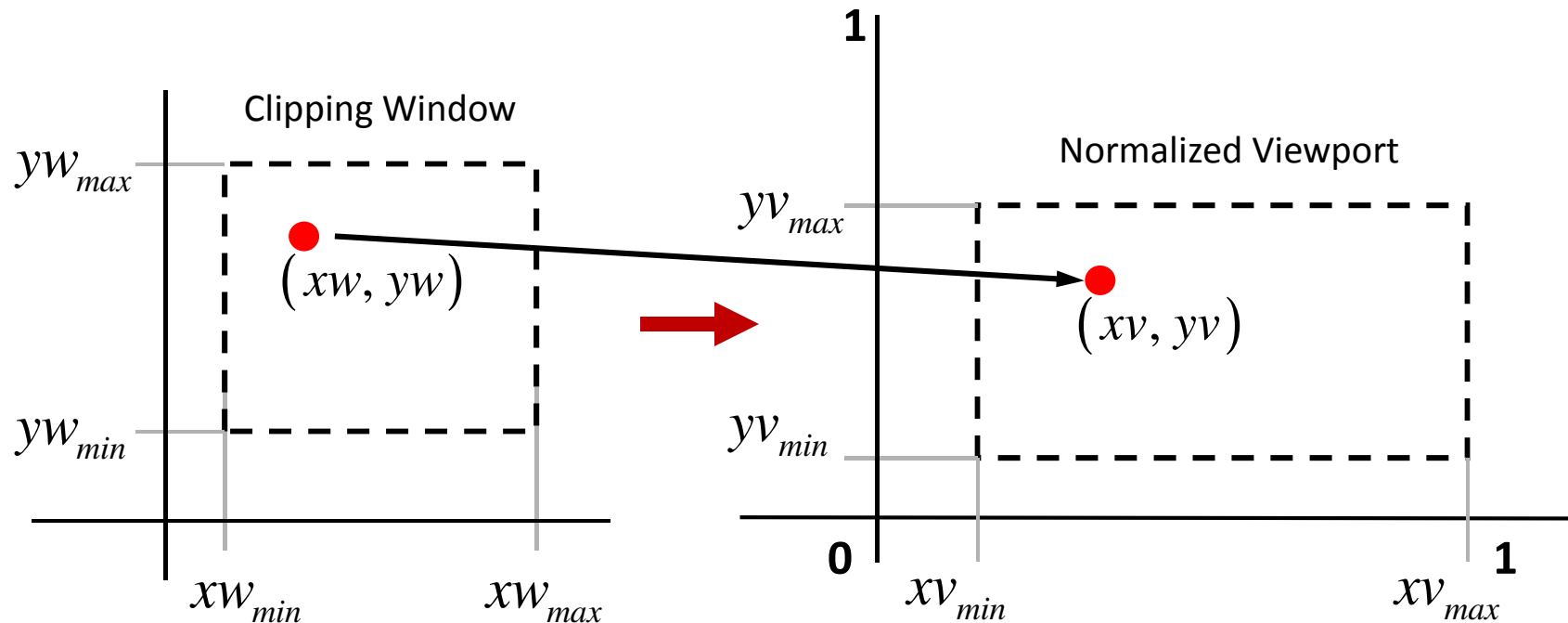
- The steps in this coordinate transformation
 - A viewing coordinate frame is moved into coincidence with the world frame in two steps
 - a) Translate the viewing origin to the world origin, then
 - b) Rotate to align the axes of the two systems



Normalization and Viewport Transformations

- First approach:
 - Normalization and window-to-viewport transformations are combined into one operation.
 - Viewport range can be in $[0,1] \times [0,1]$.
 - Clipping takes place in $[0,1] \times [0,1]$.
 - Viewport is then mapped to display device.
- Second approach:
 - Normalization and clipping take place before viewport transformation.
 - Viewport coordinates are specified in screen coordinates.

Mapping the Clipping Window into a Normalized Viewport



Maintain relative size and position between clipping window and viewport.

To transform WC point into the same relative position within the viewport, we require that:

$$\frac{xv - xv_{\min}}{xv_{\max} - xv_{\min}} = \frac{xw - xw_{\min}}{xw_{\max} - xw_{\min}} \quad \frac{yv - yv_{\min}}{yv_{\max} - yv_{\min}} = \frac{yw - yw_{\min}}{yw_{\max} - yw_{\min}}$$

Solving for (xv, yv) obtains:

$$xv = s_x xw + t_x, \quad yv = s_y yw + t_y, \quad \text{where}$$

Scaling factors:

$$s_x = \frac{xv_{\max} - xv_{\min}}{xw_{\max} - xw_{\min}}, \quad s_y = \frac{yv_{\max} - yv_{\min}}{yw_{\max} - yw_{\min}}$$

Translation factors:

$$t_x = \frac{xw_{\max} xv_{\min} - xw_{\min} xv_{\max}}{xw_{\max} - xw_{\min}}, \quad t_y = \frac{yw_{\max} yv_{\min} - yw_{\min} yv_{\max}}{yw_{\max} - yw_{\min}}$$

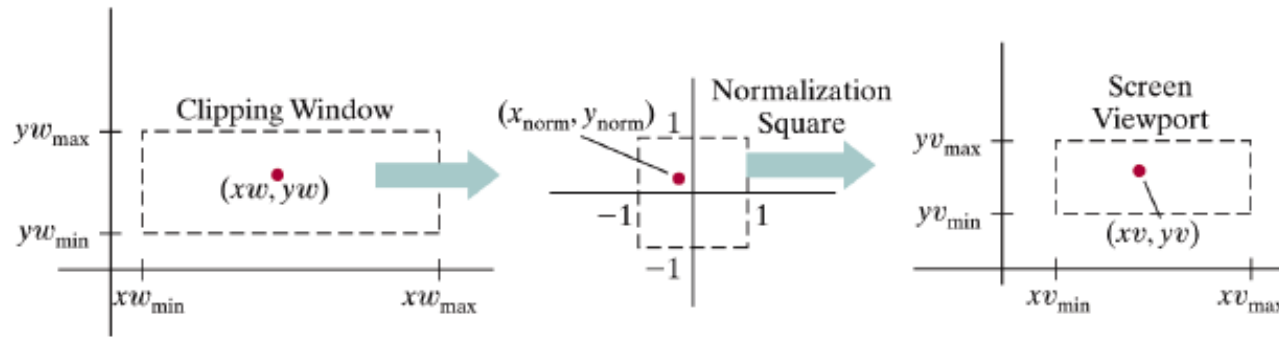
Composite matrix representation for the transformation to the normalized viewport:

$$\mathbf{M}_{\text{window, norm_viewport}} = \begin{bmatrix} s_x & 0 & t_x \\ 0 & s_y & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

- Conversion sequence of transformation:
 1. Perform a scaling transformation using a fixed-point position of (xw_{\min}, yw_{\min}) that scales the window area to the size of the viewport
 1. Translate the scaled window area to the position of the viewport

$$\mathbf{M}_{\text{window, norm_viewport}} = \begin{bmatrix} s_x & 0 & t_x \\ 0 & s_y & t_y \\ 0 & 0 & 1 \end{bmatrix}$$

Mapping the Clipping Window into a Normalized Square



$$\mathbf{M}_{\text{window, norm_square}} = \begin{bmatrix} \frac{2}{xw_{\max} - xw_{\min}} & 0 & -\frac{xw_{\max} + xw_{\min}}{xw_{\max} - xw_{\min}} \\ 0 & \frac{2}{yw_{\max} - yw_{\min}} & -\frac{yw_{\max} + yw_{\min}}{yw_{\max} - yw_{\min}} \\ 0 & 0 & 1 \end{bmatrix}$$

$$\mathbf{M}_{\text{norm_square, viewport}} = \begin{bmatrix} (xv_{\max} - xv_{\min})/2 & 0 & (xv_{\max} + xv_{\min})/2 \\ 0 & (yv_{\max} - yv_{\min})/2 & (yv_{\max} + yv_{\min})/2 \\ 0 & 0 & 1 \end{bmatrix}$$